

DO NOW

Get a laptop and get logged on.

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3.1 Derivatives Introduction - Day 3

Finding the equation of the tangent line at a given point:

- Find $f'(x)$
- Find slope at that point
- Use $y - y_1 = m(x - x_1)$

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Example: $f(x) = x^2 - 3$

Find the equation of the tangent line at the point (2, 1)

$$\begin{aligned} \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{(x+\Delta x)^2 - 3 - (x^2 - 3)}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x + (\Delta x)^2 - 3 - x^2 + 3}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{2x\Delta x + (\Delta x)^2}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} 2x + \Delta x \end{aligned}$$

$$\begin{aligned} f'(x) &= 2x \\ f'(2) &= 2(2) \\ m &= 4 \end{aligned}$$

equation:

$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y - 1 &= 4(x - 2) \\ y - 1 &= 4x - 8 \\ \boxed{0 = 4x - y - 7} \end{aligned}$$

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Example: $f(x) = 2x^2 - 5$

Find the equation of the tangent line at the point (2, 3)

$$\begin{aligned} \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{2(x+\Delta x)^2 - 5 - (2x^2 - 5)}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{2(x^2 + 2x\Delta x + (\Delta x)^2) - 5 - 2x^2 + 5}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{2x^2 + 4x\Delta x + 2(\Delta x)^2 - 5 - 2x^2 + 5}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} \frac{4x\Delta x + 2(\Delta x)^2}{\Delta x} \\ \lim_{\Delta x \rightarrow 0} 4x + 2\Delta x \end{aligned}$$

$$\begin{aligned} f'(x) &= 4x \\ f'(2) &= 4(2) = 8 \end{aligned}$$

equation

$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y - 3 &= 8(x - 2) \\ y - 3 &= 8x - 16 \\ \boxed{0 = 8x - y - 13} \end{aligned}$$

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Identify the derivative graphs

Draw the derivative graph

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HOMEWORK

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